



# CE 416 Reinforced Concrete Design – II

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CE 416: Reinforced Concrete Design - II

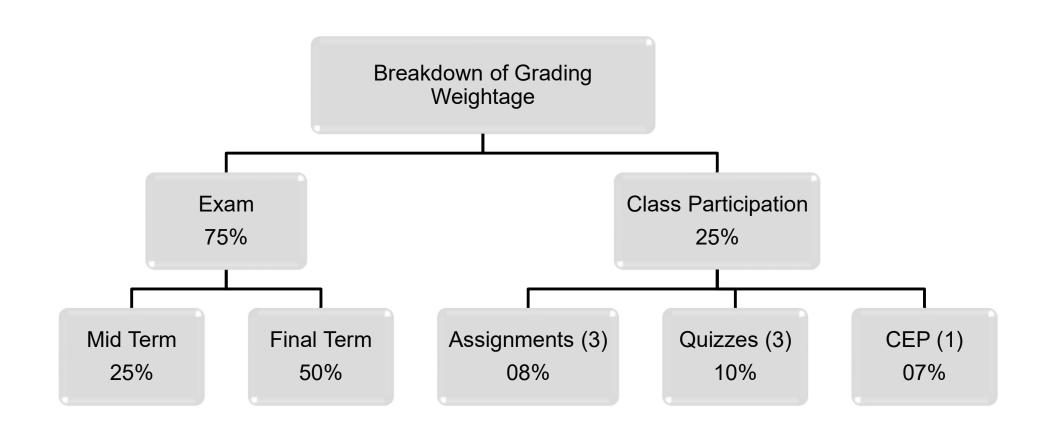


#### **Course Contents**

**OBE Course Contents Fall 2023** 



### **Grading Policy**





### **Teaching Plan**

Week	Lectures	Assessments				
01	Lecture 1: Introduction					
02	Lecture 2 Part_I: Analysis and Design of One-way Slab					
	System					
03	-Do-	Assignment#1				
04	Lecture 2 Part_II: Analysis and Design of One-way Slab					
04	System					
	Lecture 3: Analysis and Design of Two-way Slab					
05	Systems (Two Way Slabs Supported on Stiff Beams Or					
	Walls)					
06	-Do-	Quiz #1				
	Lecture 4: Analysis and Design of Two-way Slab System					
07	without Beams (Flat Plates and Flat Slabs)	Assignment#2				
08	-Do-					
09	Mid Term Examination					



### **Teaching Plan**

Week	Lectures	Assessments			
10	Lecture 5 Part_I: Introduction to Earthquake Resistant	Accianmont#2			
10	Design of Reinforced Concrete Structures	Assignment#3			
11	Lecture 5 Part_II: Introduction to Earthquake Resistant	Quiz #2			
	Design of Reinforced Concrete Structures				
12	Lecture 6: Design of RC Retaining Walls				
13	-Do-				
14	Lecture 7: Introduction to Bridge Engineering				
15	Lecture 8: Introduction to Prestressed Concrete	Quiz #3			
16	Final Term Examination				



### **Lecture Availability**

• You can access previous versions of lectures on my website at the following link :

#### https://drqaisarali.com/lectures/.

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				Lecture 1 Introduction (Color version) (Black & White vers	sion)							

 Updated lectures upon completion will be uploaded on website as well as on Google Classroom.



# Lecture 01 Introduction

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### **Learning Outcomes**

- At the end of this lecture, students will be able to;
  - > *Explain* Difference between Demand and Capacity
  - > **Compare** Working stress method with Strength Design method
  - Analyze and Design Beams for flexure and shear using ACI Recommendations

### **Lecture Contents**

- Concept of Demand and Capacity
- A Glimpse of RCD I
  - Load Combinations and Strength Reduction Factors
  - ACI Code Provisions related to Flexural Design of beams
  - ACI Code Provisions related to Shear Design of beams
- Flexural and Shear Design of Beam (Example)
- References
- Appendix



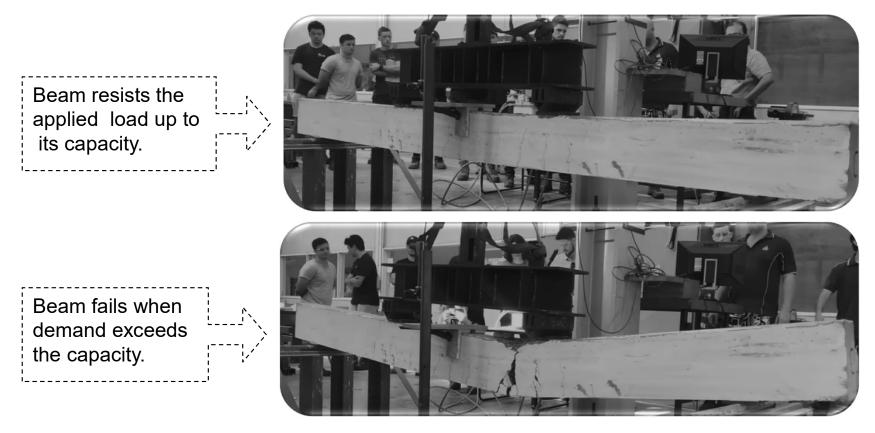
#### Demand

- Demand on a structure refers to all external actions.
- Gravity, wind, earthquake, snow are external actions.
- These actions when act on the structure will induce internal disturbance(s) in the structure in the form of stresses (such as compression, tension, bending, shear and torsion).
- The internal stresses are also called Load effects.



#### □ Capacity

• Capacity refers to the overall ability of a structure to carry an imposed demand.





#### □ Failure

- Failure occurs when Capacity is less than Demand.
- To avoid failure, capacity to demand ratio should be kept greater than one, or at least equal to one.
- It is, however, intuitive to have some margin of safety i.e., to have capacity to demand ratio more than one. How much?



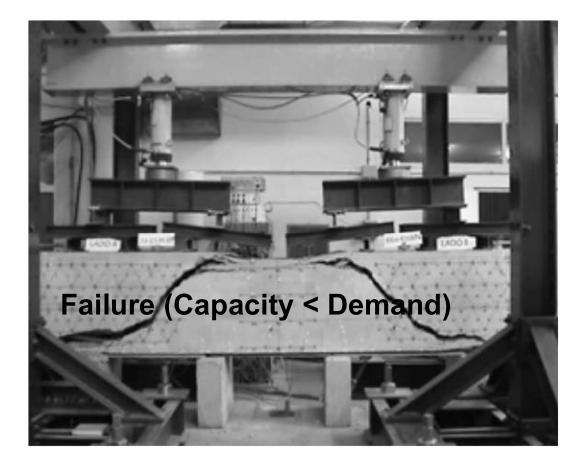
#### □ Failure

An Experimental Test on Beam's Capacity under Point load

Depth =12 in Width = 8 in Length =7 ft Bars = 4,#4 Stirrup Spacing =5 in c/c Calcullted Load Capicty=90 KN



#### □ Failure





#### □ About Ton

• **Ton** is the name which basically describes the unit of weight. Different types of Ton are tabulated below.

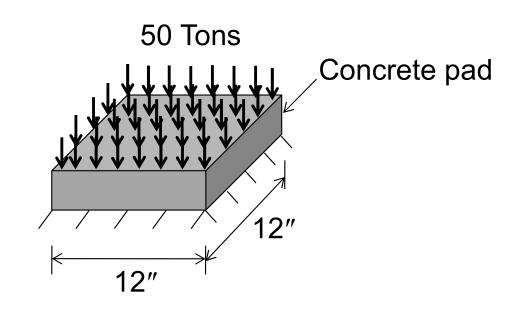
S. No.	Name	Quantity	
1	Long Ton (US)	2240 pounds	
2	Short Ton (US) 2000 pounds		
3	Tonne or Metric Ton	2204.6226 pounds Or 1000kg	

• In Pakistan, the use of metric ton is very common; therefore; we will refer to Metric Ton in our discussion.



#### Example 1.1

 Calculate demand in the form of stresses or load effects on the given concrete pad of size 12" × 12".





#### □ Solution

- Given Data
  - Load, P = 50 Tones = 50 X 2204 = 110200 lb.
  - Area of concrete Pad,  $A = 12 \times 12 = 144 \text{ in}^2$
- Required Data
  - Calculate the Capacity of Concrete Pad for the given Demand



#### □ Solution

 Based on convenience either the loads or the load effects as demand are compared to the load carrying capacity of the structure in the relevant units.

As we know that

 $Capacity = Strength \times Area \Rightarrow C = \sigma_{max} \times A$ 

For concrete pad;  $\sigma_{max} = f_s$ 

 $C = f_s \times 144$ 



#### □ Solution

• For safety, Capacity should be equal to or greater than demand.

For *Capacity* = *Demand*;

$$f_s \times 144 = 110200$$

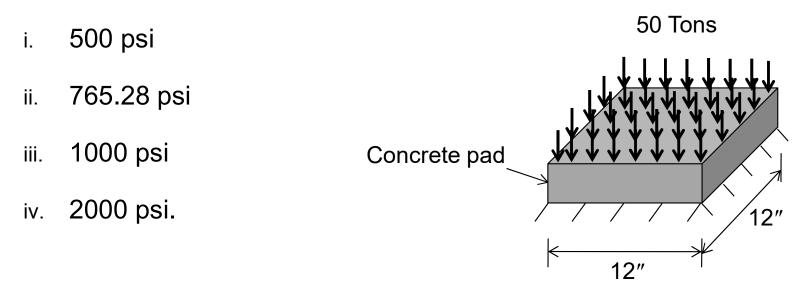
$$f_s = \frac{110200}{144} = 765.28psi$$

- This means Capacity of the pad in the form of resistance should be able to carry a stress of 765.28 psi.
- In other words, the compressive strength of concrete pad (capacity) should be more than 765.28 psi (demand).



#### **Example 1.2**

• Determine capacity to demand ratio for the pad of example 1.1 for the following capacities given in the form of compressive strength of concrete. Comment on the results





#### □ Solution

Part	Capacity/Demand	Remarks	
i	500/765.28 = 0.7	Capacity is less than Demand	
ii	765.28/765.28 = 1.0	Capacity is just equal to Demand	
iii	1000/765.28 = 1.3	Capacity is 1.3 times greater than Demand	
iv	1200/765.28 = 1.6	Capacity is 1.6 times greater than Demand	

• In (iii) and (iv), there is some margin of safety normally called as factor of safety.



#### □ Factor of Safety

- The factor by which the capacity exceeds the demand is known as Factor of Safety.
- It is always better to have a factor of safety in our designs.
- It can be achieved easily if we fix the ratio of capacity to demand greater than 1.0, say 1.5, 2.0 or so, as shown in example 1.2.



#### □ Factor of Safety

- For certain reasons, however, let say we insist on a factor of safety such that capacity to demand ratio remains 1.0. Then there are three ways of doing this:
  - 1. Take an increased demand instead of actual demand (load), e.g., 70 ton instead of 50 ton in the previous example,
  - 2. Take a reduced capacity instead of actual capacity such as 1500 psi for concrete whose actual strength is 3000 psi
  - 3. Doing both.
- How are these three situations achieved?



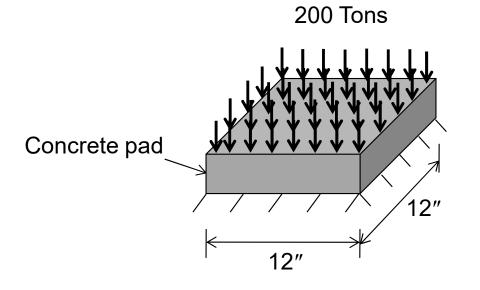
#### □ Factor of Safety

- Following are the two methods of achieving appropriates factor of safety in Design.
- 1. Working Stress Method
  - In the Working Stress or Allowable Stress Design method, the material strength is knowingly taken less than the actual one.
- 2. Strength Design Method
  - In the Strength Design method, the increased loads and the reduced strength of the material are considered, but both based on scientific rationale.



#### Example 1.3

 Design the 12" × 12" pad to carry a load of 200 tons. The area of the pad cannot be increased for some reasons. Take Concrete compressive strength, fc' = 3 ksi.





#### □ Solution

- Given Data
  - Load, P = 200 Tones
  - Area of concrete Pad, A = 12 X 12 = 144 in<sup>2</sup>
  - Concrete Strength,  $f_c' = 3000 psi$
- Required Data
  - Design Concrete Pad for the given demand



#### □ Solution

• First calculate Demand in the form of load effect

$$\sigma = \frac{P}{A} = \frac{200 \times 2204}{144} = 3061.11 psi$$

• Now, determine Factor of Safety

$$FOS = \frac{C}{D} = \frac{3000}{3061.11} = 0.98 < 1$$

#### **Food for Thought**

What are some possible solutions to this problem?



#### □ Solution

- There are three possible options to resolve this problem:
  - 1. Increase area of the pad (geometry)
  - 2. Increase the strength (by using high strength concrete, steel or other material
  - 3. Using combination of steel with concrete.
- The first option is not possible as the size of pad is restricted in the given example.
- Now Let us assume that we want to use steel bar reinforcement of yield strength f<sub>y</sub> = 40 ksi. Now again calculate the capacity using Working Stress Method.



#### □ Solution

• For Demand = Capacity; and using Working Stress Method

$$P = R_c + R_s$$

$$P = \left(\frac{f_c'}{2}\right)(A_g - A_s) + \left(\frac{f_y}{2}\right)A_s$$

By Substituting the relevant values, we get

$$200 \times 2.204 = \left(\frac{3}{2}\right) \times (144 - A_s) + \left(\frac{40}{2}\right)A_s$$

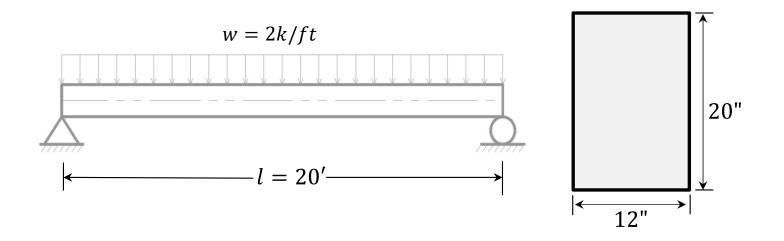
Which on solving for  $A_s$  gives

$$A_s = 12.15in^2$$



#### Example 1.4

 Check the capacity of the plain concrete beam given in figure below against flexural stresses within the linear elastic range. Concrete compressive strength (fc') = 3 ksi. Consider Self weight of the beam.





#### □ Solution

- Given Data
  - Load on beam (excluding self weight), W = 2 kip/ft
  - Width, b = 12"
  - Depth, h = 20"
  - Concrete Strength,  $f_c' = 3000 psi$
- Required Data
  - Calculate the Capacity of the beam



#### □ Solution

Step 1: Calculate Demand Moment on Beam

Self weight of beam, SW =  $\frac{12 \times 20}{144} \times 0.145 = 0.242$ kip/ft

Maximum Bending Moment at the midspan of the beam is given by;

$$M_u = \frac{W_u l^2}{8}$$
$$M_u = \frac{(2 + 0.242)20^2}{8} \times 12$$
$$M_u = 1345.2 \text{ in. kip}$$



#### □ Solution

#### Step 2: Calculate Flexural Capacity of beam

In the linear elastic range, flexural stress in concrete beam can be calculated as:

$$f = \frac{Mc}{I}$$

Where;

$$I = \frac{bh^3}{12} = \frac{12 \times 20^3}{12} = 8000 \text{ in}^4$$

and

$$c = \frac{h}{2} = \frac{20}{2} = 10$$
 in



#### □ Solution

#### Step 2: Calculate Flexural Capacity of beam

As we know that for a plain concrete beam Flexural strength is equal to modulus of rupture which is given by;

$$f = f_r = 7.5\sqrt{f_c'} = 7.5\sqrt{3000} = 410.79$$
 psi

Now,

$$M = \frac{fI}{c} = \frac{410.79 \times 8000}{10} = 328632 \text{ lb. in } or 328.63 \text{ in. kip}$$

Hence, Demand = 1345.2 in-kips and Capacity = 328.63 in-kips



## A Glimpse of RCD – I

- In RCD I, you have already studied the detailed procedure of designing Beams, Slabs, Columns and Footings.
- However, for the sake of revision, we will briefly go over some of those concepts here.

### A Glimpse of RCD – I

#### □ Load Combinations

Table 5.3.1 - Load combinations					
Load combination	Notations				
U = 1.4D					
U = 1.2D + 1.6L + 0.5 (L <sub>r</sub> or S or R)	D = Dead Load L = Live Load				
U = 1.2D + 1.6(L <sub>r</sub> or S or R) + (1.0L or 0.5W)	L <sub>r</sub> = Roof Live Load R = Rain Load				
U = $1.2D + 1.0W + 1.0L + 0.5(L_r \text{ or } S \text{ or } R)$	S = Snow Load				
U = 1.2D + 1.0E + 1.0L + 0.2S	W = Wind Load E = Earthquake Load				
U = 0.9D + 1.0W					
U = 0.9D + 1.0E					



#### □ Strength Reduction Factors

Table 21.2.1—Strength reduction factors		
S. No.	Action or structural element	φ
1	Tension controlled regions (Moment)	0.90
2	Compression controlled regions (Axial force)	0.65
3	Shear	0.75
4	Torsion	0.75



#### □ Flexural Design of Beam

• The Design Flexural Capacity of an RC beam is given by

$$\emptyset M_n = \emptyset A_s f_y \left( d - \frac{a}{2} \right)$$

$$a = \frac{A_s f_y}{0.85 f_c{'b}}$$

Where  $A_s$  which is tensile reinforcement, is subjected to the following restrictions.

 $A_{s,min} < A_s < A_{s,max}$ 

## □ Flexural Design of Beam

Minimum Reinforcement Limit

$$A_{s,min} = \frac{3\sqrt{f_c'}}{f_y} bd$$
 or  $\frac{200}{f_y} bd$  which ever is greater

Maximum Reinforcement Limit

$$A_{s,max,40} = \frac{f_c'}{136}bd$$

$$A_{s,max,60} = \frac{f_c'}{223} bd$$

#### Food for Thought

Why have these restrictions been imposed on the steel area ?

#### Shear Design of Beam

Design Shear Capacity of beam is given by

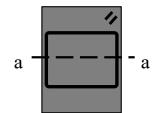
Where;

$$\emptyset V_c = 2\emptyset \sqrt{f_c'} bd$$

and

$$\emptyset V_s = \frac{\emptyset A_v f_y d}{s_d}$$

 $A_v$  is the cross-sectional area of web reinforcement within a distance "s", for single loop stirrups (2 legged),  $A_v = 2A_s$  $A_s$  = cross sectional area of the stirrup bar



At section a-a, if #3 bar is used  $A_s = 0.11$ in<sup>2</sup>,  $A_v = 2 \times 0.11 = 0.22$  in<sup>2</sup>



#### □ Shear Design of Beam

- The beam is designed for the ultimate shear force  $V_u$  at critical location (which in most cases is at a distance "d" from the face of support.)
- 1. When  $\emptyset V_c / 2 > V_u$ , no web reinforcement is required.
- 2. When  $\emptyset V_c \ge V_u$  but  $\emptyset V_c / 2 < V_u$ , theoretically no web reinforcement is required. However, minimum web reinforcement in the form of maximum spacing  $S_{max}$  shall be provided:

$$s_{max} = \text{minimum of} \left\{ \frac{A_v f_y}{50b_w}, \frac{A_v f_y}{0.75\sqrt{f_c'}b_w}, \frac{d}{2}, 24'' \right\}$$

### □ Shear Design of Beam

- 3. When  $\emptyset V_c < V_u$ , web reinforcement is required.
  - In this case, the required spacing  $s_d$  can be calculated using

$$s_d = \frac{\emptyset A_v f_y d}{V_u - \emptyset V_c}$$

• If  $s_d$  is greater than  $s_{max}$ , use  $s_{max}$ 

## □ Shear Design of Beam

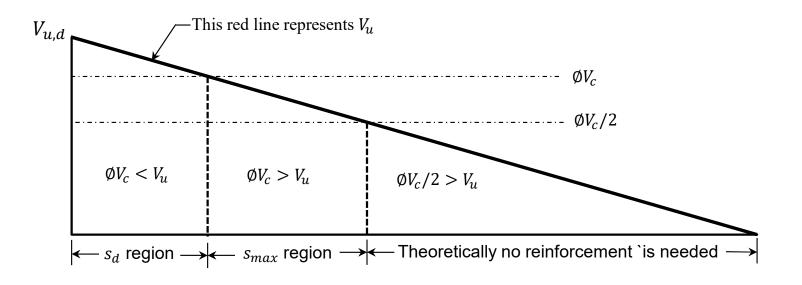
- Necessary Checks
  - 1. Check for Depth of Beam

 $\emptyset V_s \leq \emptyset 8 \sqrt{f_c'} b_w d \rightarrow \text{Depth of beam is OK!, otherwise increase depth}$ 

#### 2. Check for maximum Spacing of stirrups

 $\emptyset V_s \le \emptyset 4 \sqrt{f_c'} b_w d \rightarrow S_{max}$  is OK!, otherwise divide  $S_{max}$  by 2

#### □ Shear Design of Beam



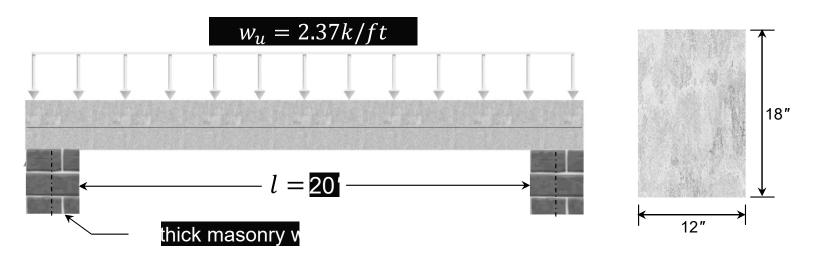
- For  $\emptyset V_c < V_u \rightarrow \text{use } s_d$
- For  $\emptyset V_c > V_u$ , use  $s_{max}$
- For  $\delta V_c/2 > V_u$ , no reinforcement is required



### Example 1.5

 A simply supported beam with given cross sectional dimensions is subjected to a uniformly distributed factored load of 2.37 kip/ft as shown in the figure below.

*Analyze* and *Design* the beam for flexure and shear in accordance with ACI 318-19. Take  $f_c' = 3ksi$  and  $f_y = 40ksi$ 

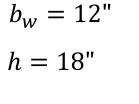




#### Solution

Step 1: Selection of sizes

Cross sectional dimensions are already given



Assuming  $\bar{y} = 2.5$ "

d = 18 - 2.5 = 15.5"

Step 2: Calculation of loads

 $w_u = 2.37k/ft$ 



#### □ Solution

- Step 3: Analysis
  - 1. Analysis for Flexure

$$M_u = \frac{w_u l^2}{8} = \frac{2.37(20.75)^2}{8} \times 12 = 1530.65 \text{ in. kip}$$

1. Analysis for Shear

From eq.(6.5), we have  $V_u = w_u (l_n/2 - d)$   $V_u = 2.37(20/2 - 15.5/12)$  $V_u = 20.64$  kips



## □ Solution

#### Step 4: Determination of flexural steel area

Using direct method, we have

$$a = 15.5 - \sqrt{15.5^2 - \frac{2.614 \times 1530.65}{3 \times 12}} = 4.1''$$

Putting a = 4.14" and  $\emptyset = 0.90$ , we get

$$A_s = \frac{M_u}{\emptyset f_y (d - \frac{a}{2})} = \frac{1530.65}{0.9 \times 40 \left(15.5 - \frac{4.14}{2}\right)}$$
$$A_s = 3.17 \ in^2$$



### □ Solution

- > Step 5: Check for flexural steel area
  - Minimum reinforcement limit

$$A_{s,min} = \frac{200}{f_y} b_w d = \frac{200}{40000} \times 12 \times 15.5 = 0.93 \ in^2$$

• Maximum reinforcement limit

$$A_{s,max} = \frac{f_c' b_w d}{136} = \frac{3 \times 12 \times 15.5}{136} = 4.1 \ in^2$$

$$A_{s,min} < A_s < A_{s,max} \Rightarrow OK!$$



## □ Solution

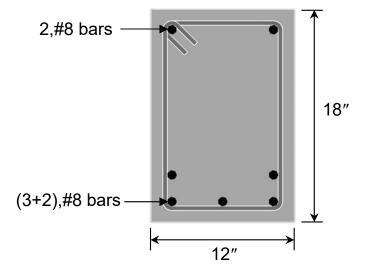
Step 6: Detailing of flexural reinforcement

Using #8 bar with  $A_b = 0.79in^2$ 

*No. of bars* 
$$= \frac{A_s}{A_b} = \frac{3.17}{0.79} = 4.01 \approx 5$$

Provide 5,#8 bars in two layers

- 3 in first layer and
- 2 in second layer





## □ Solution

#### Step 7: Check for requirement of Shear reinforcement

From eq.(6.2), Design shear capacity of concrete can be calculated as;

 $ØV_c = 15.28k$ 

 $\emptyset V_c < V_u = 20.64 \ k \rightarrow$  Shear reinforcement is required.



## □ Solution

#### Step 8: Determination of stirrup spacing

Calculate design spacing  $s_d$  using eq. (6.4)

$$s_d = \frac{\emptyset A_v f_y d}{V_u - \emptyset V_c}$$

Using 2 legged #3 stirrups,  $A_v = 2A_b = 2(0.11) = 0.22in^2$ 

$$s_d = \frac{0.75 \times 0.22 \times 40 \times 15.5}{20.64 - 15.28}$$

 $s_d = 19.1"$ 



## □ Solution

#### Step 8: Determination of stirrup spacing

Calculate maximum spacing  $s_{max}$  using eq. (6.6)

$$s_{max} = Least \ of \left\{ \begin{array}{l} \frac{A_v f_y}{50b_w} = \frac{0.22 \times 40,000}{50 \times 12} = 14.67" \\ \frac{A_v f_y}{0.75 \sqrt{f_c}' b_w} = \frac{0.22 \times 40,000}{0.75 \sqrt{3000} \times 12} = 17.85" \\ \frac{d}{2} = \frac{15.5}{2} = 7.75" \\ 24" \end{array} \right.$$

 $s_{max} = 7.75'' < s_d$ 



## □ Solution

- > Step 9: Apply necessary checks
  - 1. Check for Depth of Beam

$$\emptyset V_s \le \emptyset 8 \sqrt{f_c'} b_w d$$

$$\emptyset V_s = \frac{\emptyset A_v f_y d}{s} = \frac{0.75 \times 0.22 \times 40 \times 15.5}{7.5} = 13.64 \text{ kip}$$
$$\emptyset 8 \sqrt{f_c} b_w d = 4 \emptyset V_c = 4 \times 15.28 = 61.12 \text{ kip} > \emptyset V_s \to 0K!$$

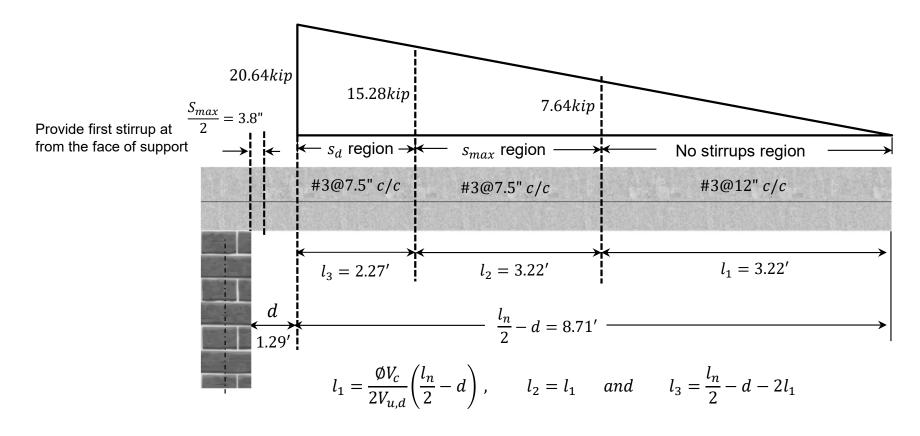
2. Check for Maximum spacing of stirrups

$$\emptyset V_s \le \emptyset 4 \sqrt{f_c'} b_w d$$
,  $\emptyset V_s = 13.64 kip$   
 $\emptyset 4 \sqrt{f_c'} b_w d = 2 \emptyset V_c = 2 \times 15.28 = 30.56 kip > \emptyset V_s \rightarrow OK!$ 



#### Solution

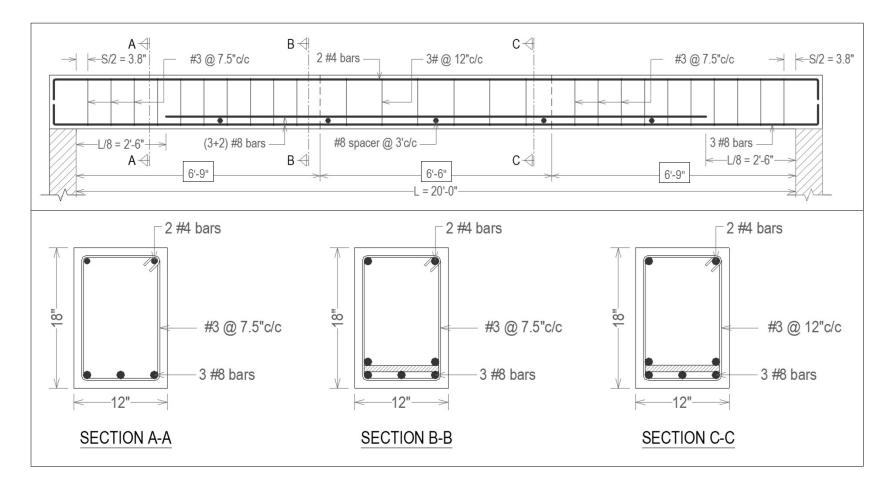
Step 10: Detailing of shear reinforcement





## □ Solution

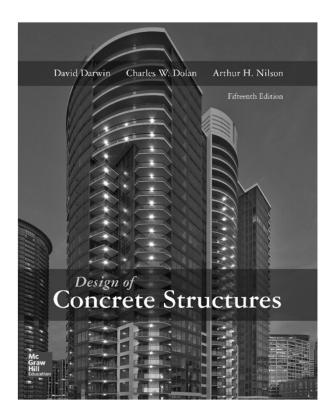
• Step 11: Drafting





## References

- Design of Concrete Structures 14th / 15th edition by Nilson, Darwin and Dolan.
- Building Code Requirements for Structural Concrete (ACI 318-19)

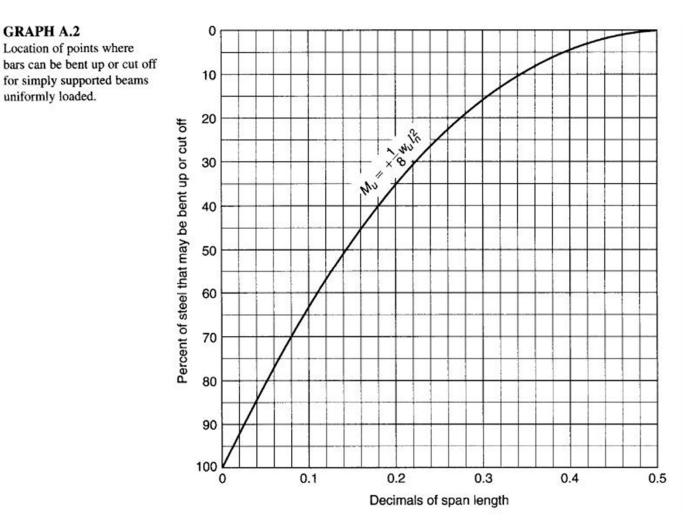


IN-LB Fab Point Univ	
An ACI Standard	
Building Code Requirements for Structural Concrete (ACI 318-19)	
Commentary on Building Code Requirements for Structural Concrete (ACI 318R-19)	
Reported by ACI Committee 318	

Updated: Sept 28, 2023 De



# Appendix

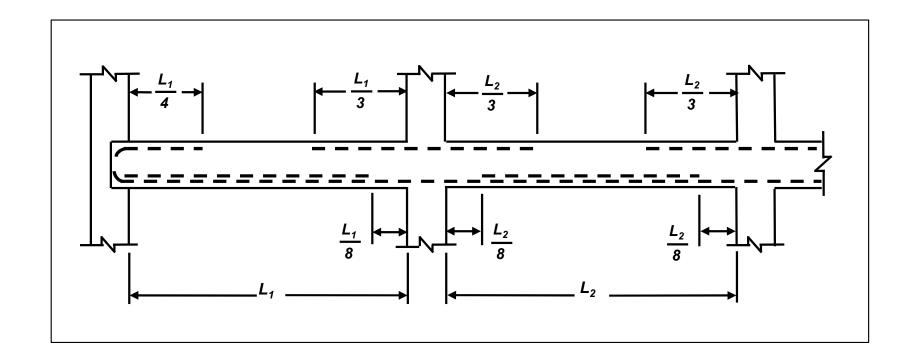


Exact curtailments lengths for simply supported positive moments (to be measured from face of the support)

Updated: Sept 28, 2023 Department of Civil Engineering, University of Engineering and Technology Peshawar, Pakistan







Cutoff for bars in approximately equal spans with uniformly distributed loads for 50% curtailment