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Lecture 02

Design of One-way Slab System (Part – II)

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CE 416: Reinforced Concrete Design - II

Updated: Oct 25, 2023 Department of Civil Engineering, University of Engineering and Technology Peshawar, Pakistan



Design of 90' X 60' Hall

Option 2a

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Solution [option 2a]

✤ Given Data

Dimensions of Hall : 90' x 60' (interior)

Story height, h = 20'

SDL: 3" Mud layer and 2" Tile layer

Live load: 40 psf

 $f_c' = 3$ ksi

 $f_y = 60$ ksi

 $q_a = 2.204 \text{ ksf}$

Required Data

Design the hall



Solution [option 2a]

Step 1: Selection of Structural Configuration





Solution [option 2a]

Step 1: Selection of Structural Configuration





Solution [option 2a]

- ✤ Slab Design
- Step 2: Selection of Sizes

 $h_{min} = 5.4$ ". Finally take h = 6"

Step 3: Calculation of Loads

 $W_u = 0.214 \text{ ksf}$

(Same as that of Part I of this lecture)

(Same as that of Part I of this lecture)



- **Solution** [option 2a]
 - ✤ Slab Design
 - Step 4: Analysis
 - Using ACI Approximate coefficients, the results obtained are shown in figure.



[1] For calculating negative moments, l_n shall be the average of the adjacent clear span lengths (ACI:6.5.2)



Solution [option 2a]

- ✤ Slab Design
- > Step 5: Determination of flexural steel area

Calculate moment capacity provided by minimum reinforcement

$$A_{s,min} = 0.129 \text{ in}^2/\text{ft}$$

Finally provide #3 @ 9" c/c for both main and shrinkage bars.



- **Solution** [option 2a]
 - ✤ Slab Design
 - Step 7: Drafting





- **Solution** [option 2a]
 - ✤ Slab Design
 - Step 7: Drafting





Solution [option 2a]

- ✤ Beam Design
- Step 2: Selection of Sizes

Assuming 12" width of beam, The minimum depth of beam for a one end continuous beam is given by

$$h_{min} = \frac{l}{18.5} = \frac{30 + \left(\frac{9}{12}\right)}{18.5} = 1.66'$$
$$h_{min} = 19.92''$$
Take $h = 24''$

Effective depth, d = 24 - 2.5 = 21.5''



Solution [option 2a]

- ✤ Beam Design
- Step 2: Selection of Sizes

Effective width of T- beam b_f is minimum of:

$$b_w + 16h_f = 12 + 16(6) = 108'$$

$$b_w + s_w = 12 + 9 \times 12 = 120"$$

$$b_w + \frac{l_n}{4} = 12 + \frac{29.25}{4} \times 12 = 99.75'$$



Therefore, $b_f = 99.75"$



- ✤ Beam Design
- Step 3: Calculation of Loads
 - Before performing any calculations for the load on a beam, it is essential to understand the Structural Idealization.
 - For this, please pay close attention to the animation in the upcoming slides.



Structural Idealization













- ✤ Beam Design
- Step 3: Calculation of Loads





- ✤ Beam Design
- Step 4: Analysis





- ✤ Beam Design
- Step 5: Determination of Reinforcement

Flexural Reinforcement and Detailing						
Moment, in-kip	A_s , in ²	A_{min} , in ²	A _{max} , in ²	Detailing		
$M_u(+) = 2249.35$	1.96	0.86	3.47	3-#8		
$M_u(-)=2749.21$	2.7	0.86	3.47	4-#8		

Shear Reinforcement and Detailing						
<i>V_s</i> (k)	<i>V@d</i> (k)	Ø V _c (k)	S_d (in.)	S _{max} (in.)	<i>S</i> taken (in.)	
40.53	35.57	21.52	14.8	10.8	9	
Provided reinforcement satisfies necessary shear checks						



Solution [option 2a]

- ✤ Beam Design
- Step 6: Drafting



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Solution [option 2a]

- ✤ Girder Design
- Step 2: Selection of Sizes

$$h_{min,1} = \frac{l}{18.5} = \frac{30.75}{18.5} = 1.66' \text{ or } 19.9''$$

(for one end continuous members)

$$h_{min,2} = \frac{l}{21} = \frac{28.5}{21} = 1.36' \text{ or } 16.3"$$

(for both end continuous members)





Solution [option 2a]

- ✤ Girder Design
- Step 2: Selection of Sizes

Assume 18" wide web . The effective width of T – beam, b_f is minimum of:

• $b_w + 16h_f = 18 + 16(6) = 114$ "

•
$$b_w + s_w = Not applicable$$

•
$$b_w + \frac{l_n}{4} = 18 + \frac{29.25}{4} \times 12 = 105.75$$
"



Therefore, $b_f = 105.75"$



- ✤ Girder Design
- Step 3: Calculation of Loads
 - Beams load can be approximated as point loads on girder. The uniformly distributed load on girder is coming from self weight of girder rib plus weight of slab directly resting on girder.





- ✤ Girder Design
- Step 3: Calculation of Loads
 - Since the girder is subject to both uniform and pointed loads, the ACI coefficient method is not applicable here.
 - For the analysis of such cases, any elastic analysis method, such as the slope deflection method, moment distribution method, flexibility method, stiffness method, etc., may be used.



Solution [option 2a]

- ✤ Girder Design
- Step 3: Calculation of Loads
 - P is the point load on girder and is the reaction coming from the interior support of beam due to factored load. From below figure;
 P = 2(40.53) = 81.1k



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- ✤ Girder Design
- Step 3: Calculation of Loads





Solution [option 2a]

- ✤ Girder Design
- Step 3: Calculation of Loads

Self weight of girder can be calculated as follows

$$SW = \frac{18 \times (36 - 6)}{144} \times 0.150 = 0.563 k/ft$$

Load from part of slab on girder is given by

$$SDL = W_{u,slab} \times b_w = 0.214 \times \frac{18}{12}$$
$$= 0.321 \text{k/ft}$$

Now,

$$W_{u,girder} = 0.321 + 1.2(0.563) = 1 \text{ k/ft}$$





- ✤ Girder Design
- Step 4: Analysis





- ✤ Girder Design
- Step 5: Determination of Flexural Reinforcement
 - The required areas of steel for the maximum bending moments at key points are tabulated below.

Location	M _u (kip-ft)	d (in.)	b (in.)	A _s (in²)	A _{smin} (in²)	A _{smax} (in²)	Detailing
Exterior +	668.5	33.5	105.75	4.5	2.01	8.11	(3+3) - #8
Interior –	731.95	33.5	18	5.43	2.01	8.11	(5+2) - #8
Interior +	190.55	33.5	105.75	1.26	2.01	8.11	3 - #8
5.43 in ² 5.43 in ²							
A A	4.5 in ²		₇₇ D 2.1	01 in ²	G G	4.5 in ²	J



- ✤ Girder Design
- Step 6: Determination of Shear Reinforcement
 - Design shear capacity of reinforced concrete is given by

$$\emptyset V_c = 2\emptyset \sqrt{f'_c} b_w d = \frac{2 \times 0.75 \sqrt{3000} (18 \times 33.5)}{1000} = 49.54 kip$$

- Because shear force values abruptly change at each key point, calculating spacing for each demand shear is time consuming and tedious.
- Therefore, we will adopt a different strategy in this case.



Solution [option 2a]

- ✤ Girder Design
- Step 6: Determination of Shear Reinforcement

Calculate maximum spacing s_{max} using #3 bar as stirrup.

$$s_{max} = Least of$$

$$\frac{A_v f_y}{50b_w} = \frac{0.22 \times 60000}{50 \times 18} = 14.6"$$

$$\frac{A_v f_y}{0.75 \sqrt{f_c} b_w} = \frac{0.22 \times 60000}{0.75 \sqrt{3000} \times 18} = 17.8"$$

$$s_{max} = 14.6"$$

$$\frac{d}{2} = \frac{33.5}{2} = 16.8"$$

$$24"$$



Solution [option 2a]

- ✤ Girder Design
- Step 6: Determination of Shear Reinforcement

The design shear capacity provided by stirrups using the maximum spacing S_{max} is calculated as;

$$\emptyset V_s = \frac{\emptyset A_v f_y d}{S_{max}} = \frac{0.75 \times 0.22 \times 60 \times 33.5}{14.6} = 22.72 \text{ kip}$$

Now, the overall design shear capacity of the girder is given by $\emptyset V_n = \emptyset V_c + \emptyset V_s = 49.54 + 22.72 = 72.3 \text{ kip} > max. shear at A \& C.$

It means that maximum spacing of 14.6" as permitted by ACI governs between point A and C. Finally, #3@ 9" c/c will be provided.



Solution [option 2a]

- ✤ Girder Design
- Step 6: Determination of Shear Reinforcement

Calculate spacing for shear reinforcement between point C and E.

Location	V _{max} (k)	V@d (k)	ØV _c (k)	S _d (in.)	S _{max} (in.)	S taken (in.)
CD	120.73	117.5	49.54	4.9	14.6	4.5
DE	96	94	49.54	7.5	14.6	4.5

Provided shear reinforcement satisfies necessary shear checks





Solution [option 2a]

- ✤ Girder Design
- Step 7: Drafting



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- Column Design
 - Given Data
 - Size of column : $18'' \times 18''$



- Factored load = 297.8 kips (Reaction at the interior support)
- Service load = 234 kips (Reaction at the support due to service load)
- Compressive strength of concrete, $f'_c = 3 ksi$
- Yield Tensile strength of steel, $f_y = 60 \ ksi$



Solution [option 2a]

- Column Design
- Step 1 Determination of Main longitudinal reinforcement

Calculate design axial capacity of column by assuming 1% steel area and compare the calculated capacity with demand axial load

Assuming $A_{st} = 0.01 \overline{A_g}$;

 $\alpha \emptyset P_n = 0.80 \times 0.65 [0.85 \times 3 (A_g - 0.01A_g) + (60)0.01A_g] = 1.521A_g$

 $\alpha \emptyset P_n = 1.521(324) = 526.42 \text{ kip} > P_u = 297.8 \text{ kip} \rightarrow \text{OK!}$

Therefore, $A_{st} = 0.01A_q = 0.01(324) = 3.24 \text{ in}^2 (8 - \#6 \text{ bars})$


Solution [option 2a]

- Column Design
- Step 2 Determination of Spacing for shear reinforcement

Using #3 bar with $A_b = 0.11 \text{ in}^2$

i.
$$\frac{A_v f_y}{50b_w} = 0.22 \times 60,000/(50 \times 18) = 14.7''$$

ii.
$$\frac{A_v f_y}{0.75\sqrt{f_c'}b_w} = 0.22 \times 60,000 / (0.75\sqrt{3000} \times 18) = 17.9''$$

iii. $16d_b$ of longitudinal bar = $16 \ge 0.75 = 12''$

iv. 48
$$d_b$$
 of tie bar = 48 x 3/8 = 18"

v. Smallest dimension of member = 18"

 $S_{max} = 12''$. Finally use #3 ties @ 9" c/c







Solution [option 2a]

- Footing Design
 - Given Data
 - Size of column : 18" x 18"
 - Factored load = 297.8 kips
 - Service load = 234 kips
 - Compressive strength of concrete, $f_c' = 3$ ksi
 - Yield Tensile strength of steel, $f_{\gamma} = 60$ ksi
 - Allowable bearing capacity of soil, $q_a = 2.204$ ksf
 - Depth of footing from base level, Z = 5'



Solution [option 2a]

Footing Design

STEP WISE ANALYSIS

Estimation of footing thickness and \boldsymbol{d}_{avg}

Overburden pressure

Effective bearing capacity

Bearing Area

Critical shear Parameter

bo = 154.00 in

Design pressure qu							
qu =_	2.034 ksf						
Punching s	hear force V _{up}						
Vup =	276.9 kip						
Check for P	unching Shear						
ΦVcp =_	518.7 kip	→OK					
Calculation of Maximum Moment Mu							
Mu =_	4148.034 in.kip						



Solution [option 2a]

Footing Design

Using Direct Method;

$$a = d - \sqrt{d^2 - \frac{2.614M_u}{f_c'B}} = 20.5 - \sqrt{20.5^2 - \frac{2.614 \times 4148.03}{3 \times (146)}} = 0.61"$$

$$A_s = \frac{M_u}{\emptyset f_y (d - \frac{a}{2})} = \frac{4148.03}{0.9 \times 60 \left(20.5 - \frac{0.61}{2}\right)} = 3.8 \text{ in}^2$$

Now,

 $A_{s,min} = 0.0018 Bh = 0.0018(146)(24) = 6.30 in^2$

 $A_s < A_{s,min} \rightarrow A_{s,min}$ governs



Solution [option 2a]

Footing Design

Using #4 bar with $A_b = 0.20 in^2$

$$n = \frac{6.3}{0.20} = 31.5 \approx 32$$
$$S = \frac{B - 2C_c}{n - 1} = \frac{146 - 6}{31} = 4.5'' c/c$$

Check for maximum bar spacing

 $s_{max} = Least \ of \ 3h = 3 \times 24 = 72'' \ or \ 18'' = 18''$

Provided spacing is OK!



Solution [option 2a]

Footing Design

For crack control, the maximum spacing between the adjacent bars shall not exceed S_{max} (Table 24.3.2).

$$s_{max} = \text{Least of } 15\left(\frac{40,000}{f_s}\right) - 2.5C_c \text{ and } 12\left(\frac{40,000}{f_s}\right)$$
$$f_s = \frac{2}{3}f_y = \frac{2}{3}(60,000) = 40000 \text{ psi}$$
$$s_{max} = \text{Least of } 15\left(\frac{40,000}{40,000}\right) - 2.5(3) \text{ and } 12\left(\frac{40,000}{40,000}\right) = 7.5'$$

Provided spacing of 4.5" is OK.



Solution [option 2a]

Footing Design



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Design of 90' X 60' Hall

Option 2b

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Solution [option 2b]

Step 1: Selection of Structural Configuration





Solution [option 2b]

Step 1: Selection of Structural Configuration







Solution [option 2b]

✤ Slab Design

 As seen in the figure, each slab panel is now 10 feet by 30 feet as opposed to the previous case. Because the design of a one-way slab is only dependent on the short side, the slab analysis and design will remain unchanged.

Summary of Slab Design							
Sizes h, in.	Loads W _u , (ksf)	Analysis Moment, in. kip	Ø M_{n,min} (in. kip)	Detailing of reinforcement (main and shrinkage)			
h _{min} = 4.8″ Take h = 4.8″	$W_u = 0.214$	$M_{u,ext}^{+} = 21.07$ $M_{u,int}^{-} = 18.31$ $M_{u,int}^{+} = 13.0$	33.95	#3 @9" c/c			
Drafting is same as in Option 2a							



Solution [option 2b]

- Frame Design
 - 2D frame can be detached from a 3D system as follows





Solution [option 2b]

- Frame Design
 - Analysis for Beam (using ACI Moment Coefficients)



Note: The interior support conditions of the beam (whether supported on a column or a roller) have no effect on the analysis results.



Solution [option 2b]

- Frame Design
 - Analysis for Girder





Solution [option 2b]

- Frame Design
 - Analysis for Girder





Solution [option 2b]

Frame Design

Design of Beam for Flexure							
Location	Moment in.kip	b in.	d in.	A _s in²	A _{s,min} in²	A _{s,max} in²	Detailing
Exterior support (-)	1546	12	21.5	1.42		3.47	4 - #6
Midspan (+)	1767	99.75	21.5	1.53	0.86	3.47	4 - #8
Interior Support (-)	2749	12	21.5	2.70	0.86	3.47	2 - #8

Design of Beam for Shear (same as in option 2a)							
V s (k)	<i>V@d</i> (k)	Ø V _c (k)	S _d (in.)	S _{max} (in.)	<i>S</i> taken (in.)		
40.53	35.57	21.52	14.8	10.8	9		
Provided reinforcement satisfies necessary shear checks							



Solution [option 2b]

Frame Design

Design of Girder for Flexure								
Location	M_u (in.kip)	d (in.)	b (in.)	A _s (in²)	A_{s,min} (in²)	A _{s,max} (in²)	Detailing	
Exterior +	7375.64	33.5	105.75	4.13	3.01	8.11	6 - #8	
Interior –	8712.36	33.5	18	5.38	3.01	8.11	7 - #8	
Interior +	2615.52	33.5	105.75	1.45	3.01	8.11	2 - #8	

The Shear reinforcement remain the same as in Option 2a.



Solution [option 2b]

Column Design

- Column C1 is concentric, and its design is the same as in the previous case. (slides 34–37). Columns C2 and C3 are uniaxially eccentric, so they will be designed using Design Aids.
- Design C2 by yourself. Design of C3 is carried out in the subsequent





Solution [option 2b]

Column Design





Solution [option 2b]

- Column Design
 - Determination of Longitudinal reinforcement

Taking b = h = 18" and Assuming d' = 2.5in

$$\gamma = \frac{18 - 2(2.5)}{18} = 0.72 \approx 0.70$$

$$K_n = \frac{P_u}{\phi f_c' bh} = \frac{35.25}{0.65 \times 3 \times 18 \times 18} = 0.06$$

$$R_n = \frac{M_u}{\emptyset f_c' b h^2} = \frac{1546.43}{0.65 \times 3 \times 18 \times 18^2} = 0.14$$

The relevant Design Aid from the Appendix is DA - 2.



Solution [option 2b]

- Column Design
 - Determination of Longitudinal reinforcement
 - 4. Read ρ_g from the graph

$$\rho_g = 0.018$$

 $A_{st} = 5.83 in^2$

Using #8 bar with $A_b = 0.79 in$

No. of bars = 5.83/0.79 ≈ 8

Hence Provide 12 - #8 bars



h2



Solution [option 2b]

- Column Design
 - Determination of Spacing for Shear Reinforcement

Using #3 bar with $A_b = 0.11 in^2$

i.
$$\frac{A_v f_y}{50b_w} = 0.22 \times 60,000/(50 \times 18) = 14.7''$$

ii.
$$\frac{A_v f_y}{0.75\sqrt{f_c'}b_w} = 0.22 \times 60,000 / (0.75\sqrt{3000} \times 18) = 17.9''$$

- iii. $16d_b$ of longitudinal bar = $16 \times 1 = 16''$
- iv. 48 d_b of tie bar = 48 x 3/8 = 18"
- v. Smallest dimension of member = 18"

$$S_{max} = 16''$$
. Finally use #3 ties @ 15'' c/c







Solution [option 2b]

- Footing Design
 - Design of footing for the column C1 has already been done (refer to slides 38 to 43).
 - Design footing for column C2 by yourself.
 - A summarized design of footing for C3 is shown on next slides.



Solution [option 2b]

- Footing Design
 - Given Data for C3
 - Size of column : $18'' \times 18''$
 - Factored load = 35.25 kip
 - Service load = 27.42 kip
 - Compressive strength of concrete, $f'_c = 3$ ksi
 - Yield Tensile strength of steel, $f_y = 60$ ksi
 - Allowable bearing capacity of soil, $q_a = 2.204$ ksf
 - Depth of footing from base level, Z = 5 ft.





Solution [option 2b]

- Footing Design
 - Analysis of C3 Footing



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→OK!



Solution [option 2b]

Footing Design

Using Direct Method;

$$a = d - \sqrt{d^2 - \frac{2.614M_u}{f_c'B}} = 11.5 - \sqrt{11.5^2 - \frac{2.614 \times 87.18}{3 \times (50)}} = 0.07''$$

$$A_s = \frac{M_u}{\emptyset f_y \left(d - \frac{a}{2} \right)} = \frac{87.18}{0.9 \times 60 \left(11.5 - \frac{0.07}{2} \right)} = 0.14 \text{ in}^2$$

Now,

 $A_{s,min} = 0.0018 Bh = 0.0018(50)(15) = 1.35 in^2$

 $A_s < A_{s,min} \rightarrow A_{s,min}$ governs



Solution [option 2b]

Footing Design

Using #4 bar with $A_b = 0.20 in^2$

$$n = \frac{1.35}{0.20} = 7$$
 or $S = \frac{50 - 6}{6} = 7.3$ "

Maximum spacing shall not exceed the lesser of 3h or 18".

 $S_{max} = \min(3 \times 15 = 45, 18) = 18'' \rightarrow OK$

Also, for crack control spacing shall not exceed the following

$$s_{max} = \text{Least of } 15\left(\frac{40,000}{40,000}\right) - 2.5(3) \text{ and } 12\left(\frac{40,000}{40,000}\right) = 7.5'' \to OK$$

Provided spacing is OK. Finally provide #4@6" c/c.



Solution [option 2b]

Footing Design





References

- Design of Concrete Structures 14th / 15th edition by Nilson, Darwin and Dolan.
- Building Code Requirements for Structural Concrete (ACI 318-19)





□ DESIGN AIDS (DA – 1)





□ DESIGN AIDS (DA – 2)





$\Box \text{ DESIGN AIDS (DA - 3)}$





$\Box \text{ DESIGN AIDS (DA - 4)}$





□ DESIGN AIDS (DA – 5)




Appendix

\Box DESIGN AIDS (DA – 6)



CE 416: Reinforced Concrete Design - II



Appendix

□ DESIGN AIDS (DA – 7)



CE 416: Reinforced Concrete Design - II



Appendix

□ DESIGN AIDS (DA – 8)



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